



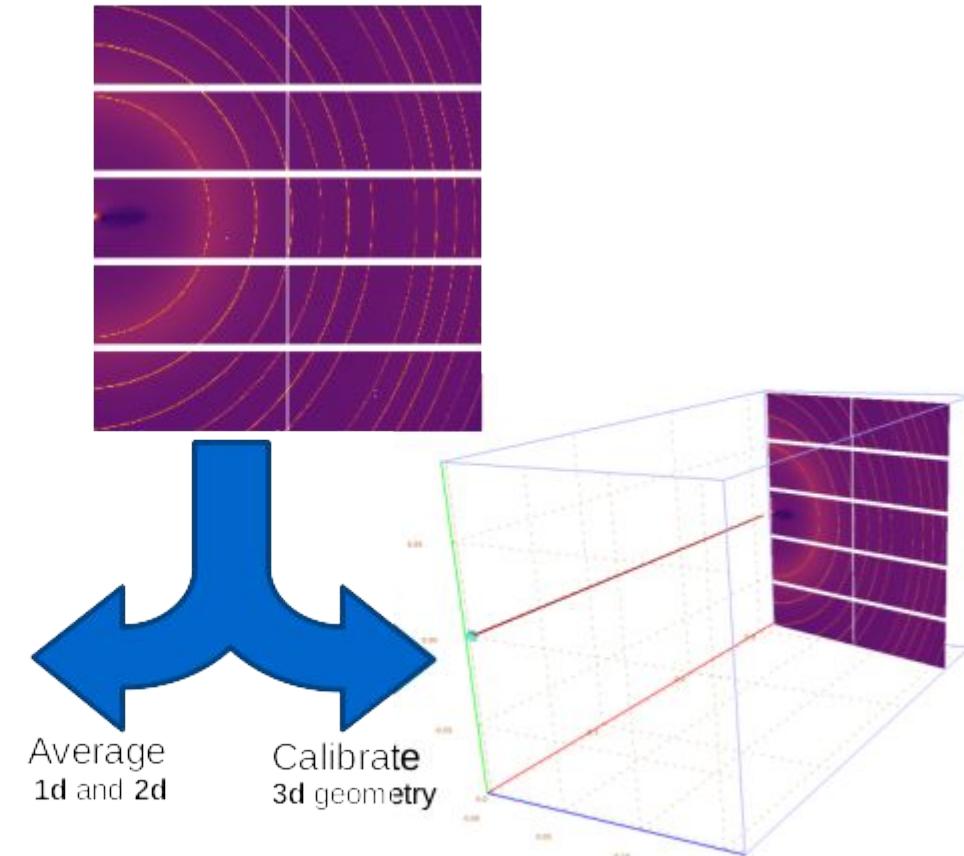
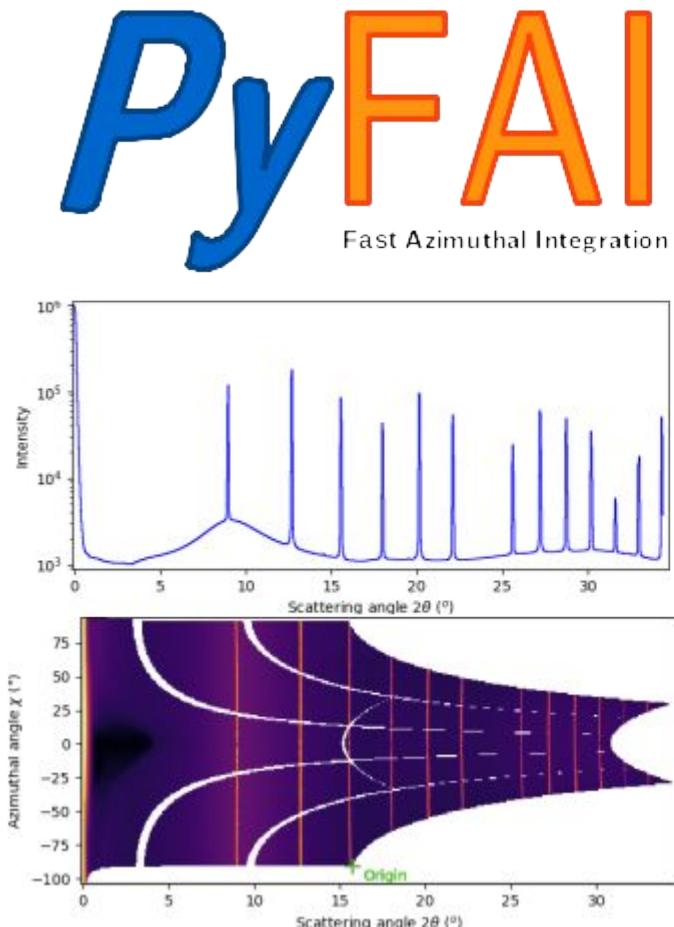
The European Synchrotron

Parallax:

A journey in sensor physics

J. Kieffer, with the input from:
G. Lotze, V. Poline, M. Ruat, P-A Douissard, M. Di Michiel,
V. Diadkin, D. Chernyshov

Fast Azimuthal Integration using Python

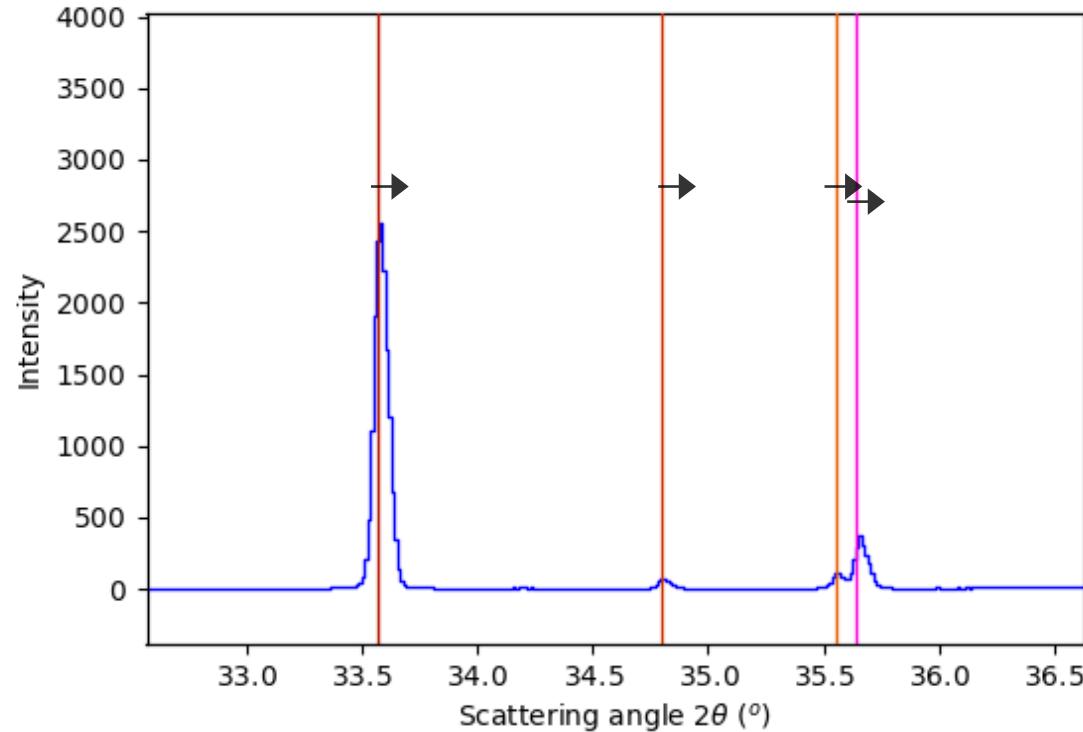
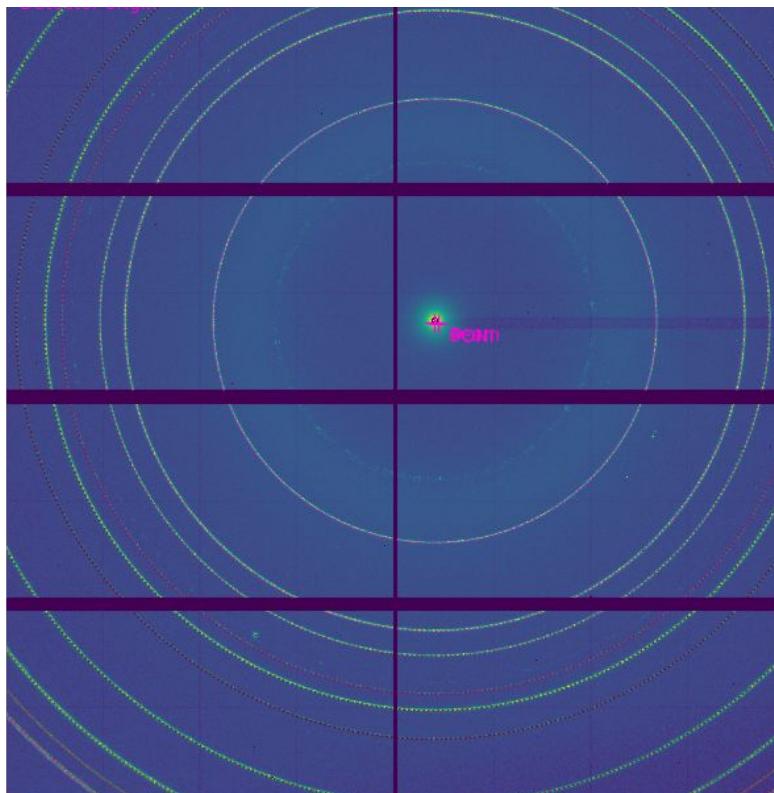


Kieffer, Jerome; Valls, Valentin; Gutierrez-Fernandez, Edgar, Ashiotis, Giannis, Karkoulis, Dimitris; Nawaz, Zubair; Deschildre, Aurore; Vincent, Thomas; Picca, Frederic Emmanuel; Massahud, Emily; Payno, Henri; Huder, Loïc; Wright, Johnathan Paul; Pandolfi, Ronald; Jankowski, Maciej; Paleo, Pierre; Faure, Bertrand; Storm, Malte; De Nolf, Wout; Wright, Christopher J.; Hopkins, Jesse B.; Pascal, Elena; Weninger, Clemens; Detlefs, Carsten; Plaswig, Florian; Lavanchy, Aurelien; gbenecke; zxs-un; iltommi11; dodogerstlin; harshal301002; Lotze, Gudrun

<https://zenodo.org/records/17984195>

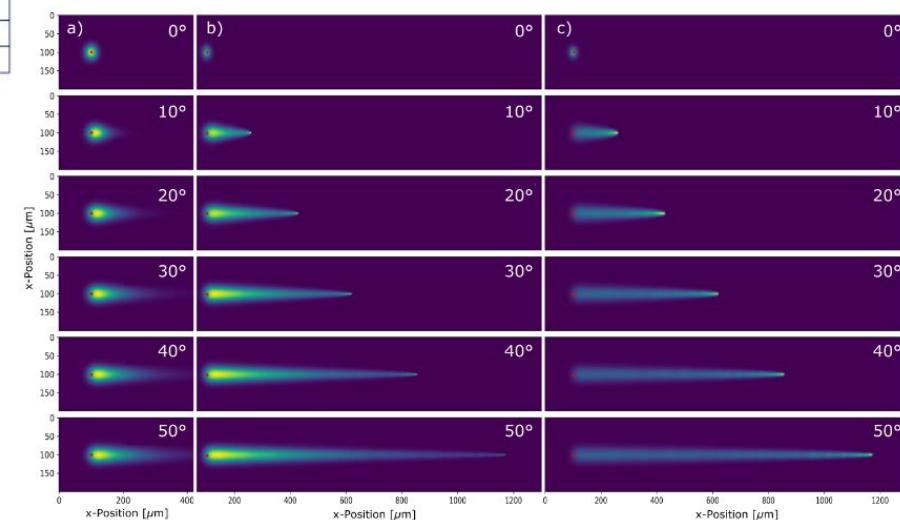
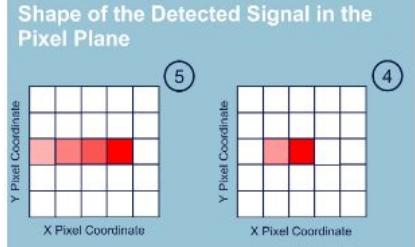
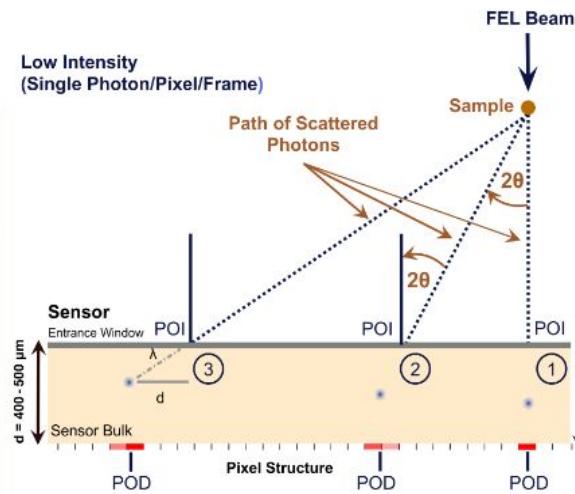
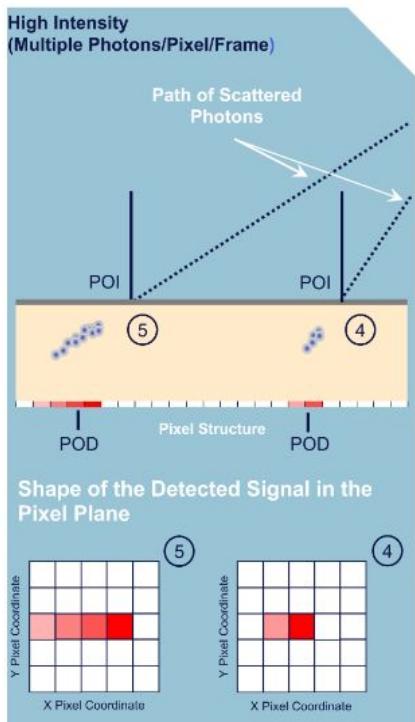
Parallax effect observed at ESRF-ID13

- **Eiger 4M detector 75 μm pixel size**
- **Silicon sensor 450 μm thickness**
- **Sample: $\alpha\text{-Al}_2\text{O}_3$ @13,45 keV**



At large incident angle ($>30^{\circ}$), photons get detected at even larger scattering angles

Parallax in photon detection



On the Influence of Parallax Effects in Thick Silicon Sensors in Coherent Diffraction Imaging

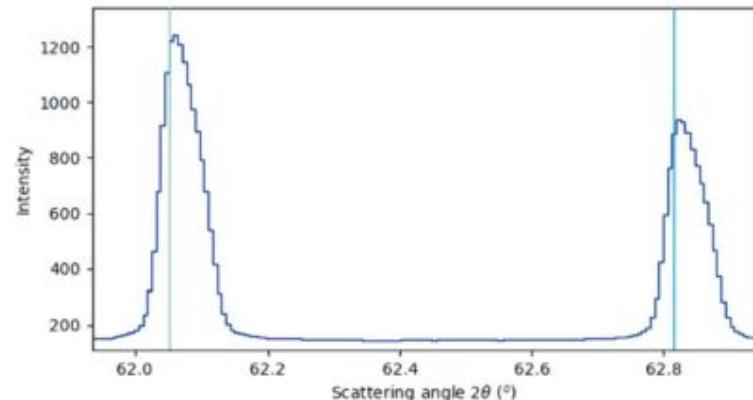
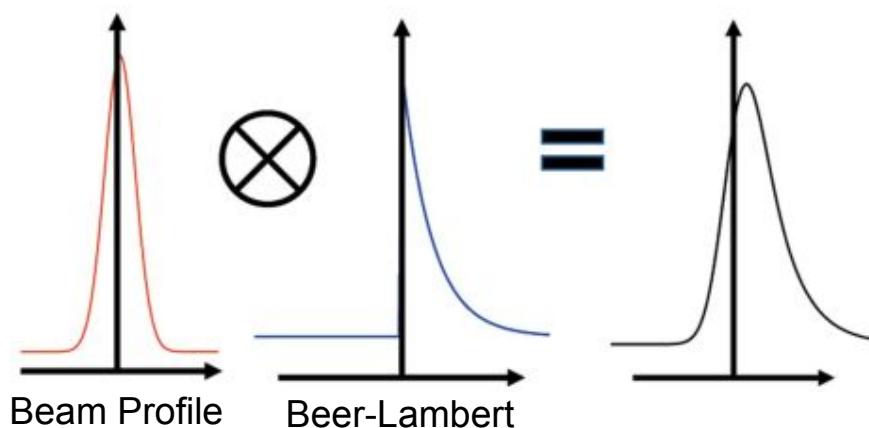
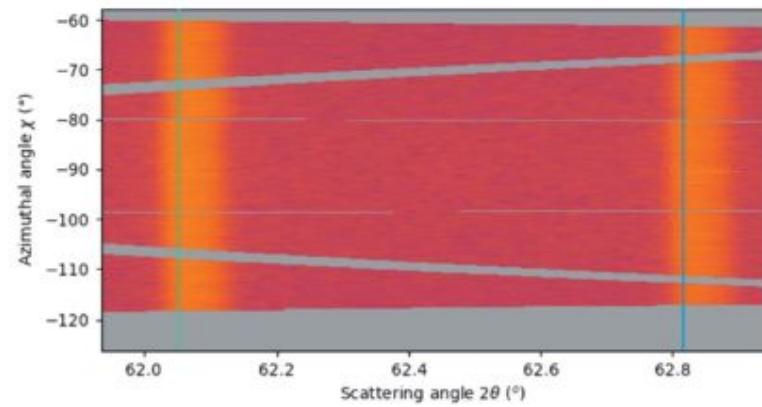
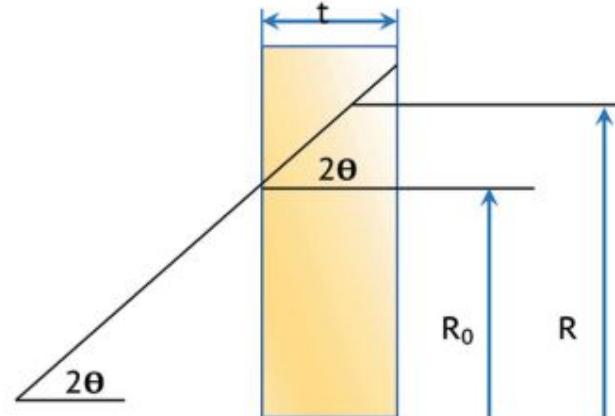
doi:10.1088/1742-6596/3010/1/012135

Beer–Lambert law:

$$-d I = \mu \cdot I \cdot d x$$

$$I = I_0 \cdot e^{-\mu \cdot r}$$

Sensor absorption convoluted with beam profile (1d)

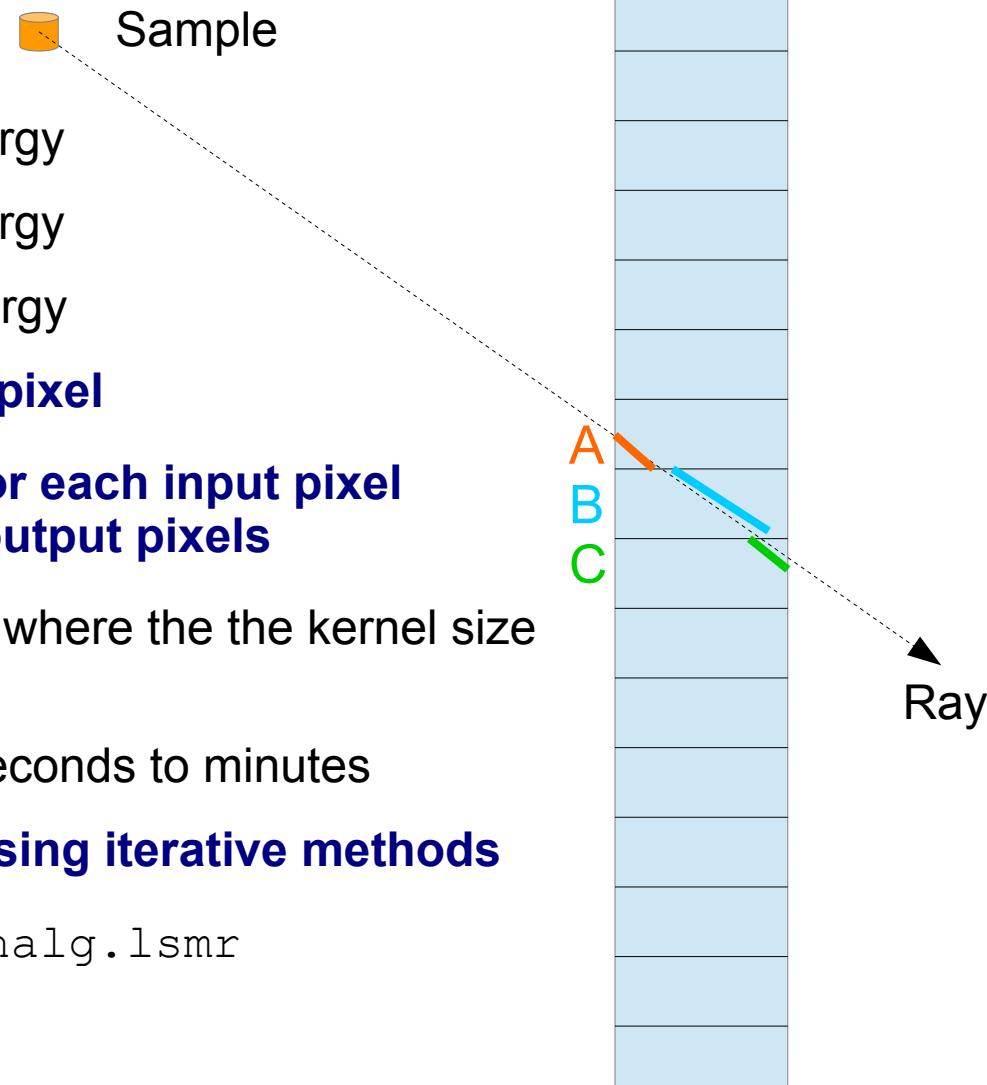


On the resolution function for powder diffraction with area detectors
<https://doi.org/10.1107/S2053273321007506>

https://github.com/silx-kit/pyFAI/blob/main/doc/source/usage/tutorial/ThickDetector/Parallax_model.ipynb

Ray-tracing of absorption in pixel depth

- **Pixels:**
 - A→Length→Deposited energy
 - B→Length→Deposited energy
 - C→Length→Deposited energy
- **Throw thousands of rays per pixel**
- **Build a (sparse) matrix with for each input pixel provides the contribution to output pixels**
 - Similar to a convolution but where the the kernel size changes from pixel to pixel
 - Matrix construction takes seconds to minutes
- **Possible to invert the effect using iterative methods**
 - Using `scipy.sparse.linalg.lsmr`
 - MLEM for poissonian data.
- **Not taking into account the integrating/counting nature of the detector**

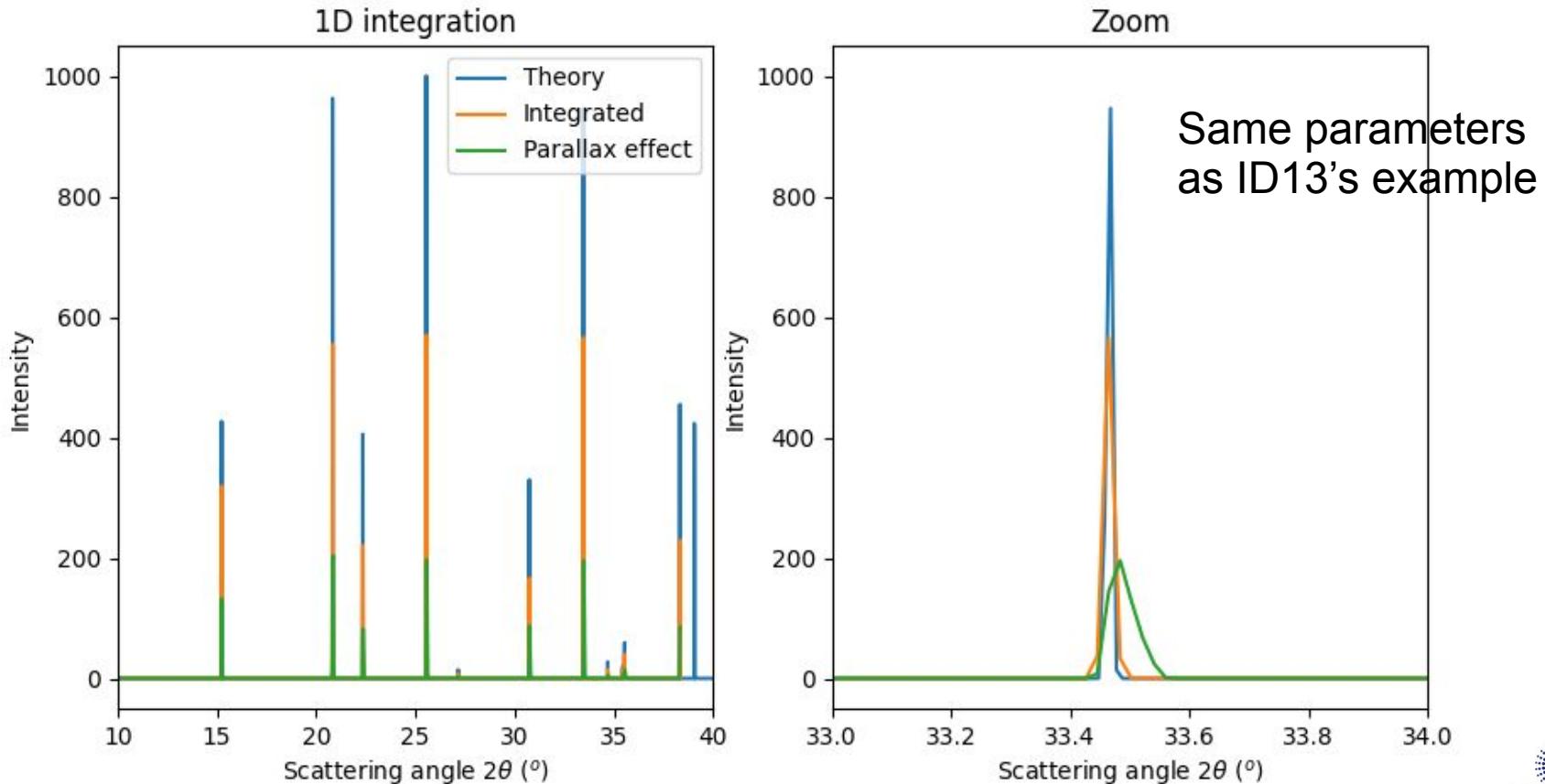


Simulation of the parallax effect in the sensor with pyFAI:

- **Based on ray-tracing:**

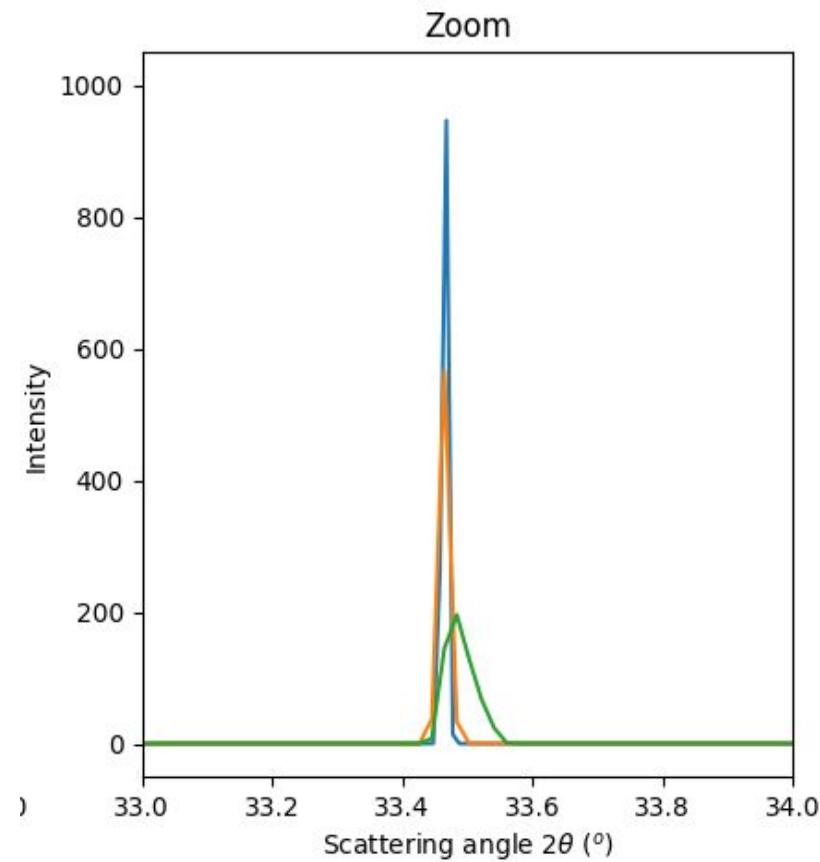
<https://github.com/silx-kit/pyFAI/blob/main/doc/source/usage/tutorial/ThickDetector/raytracing.ipynb>

- Build a blurring operator by throwing thousands of rays per pixel
- Can be used to de-convolute with iterative methods (i.e. MLEM, ...)



Exercises: Apply parallax effect on synthetic data

- **Build a synthetic geometry**
- **Create a calibrant**
- **Simulate a powder diffraction pattern and the image**
- **Perform the raytracing for the detector**
- **Blur the image**
- **Integrate the images and observe the effect of the parallax**



https://github.com/silx-kit/pyFAI/blob/main/doc/source/usage/tutorial/ThickDetector/Parallax_simple.ipynb

Different strategies to correct the effect:

- Pseudo-inversion (LSMR, MLEM, ...)
- Take into account the effect in peak-position

Thick sensor approximation: ! math !

Average value of an observable:

$$\langle x \rangle = \int_0^{\infty} x(z) \cdot P(z) dz$$

Geometrically, one has:

$$x(z) = z \cdot \tan(\alpha)$$

$P(z)$ follows Beer-Lambert law:

$$P(z) = A e^{\frac{-\mu z}{\cos(\alpha)}}$$

Normalization:

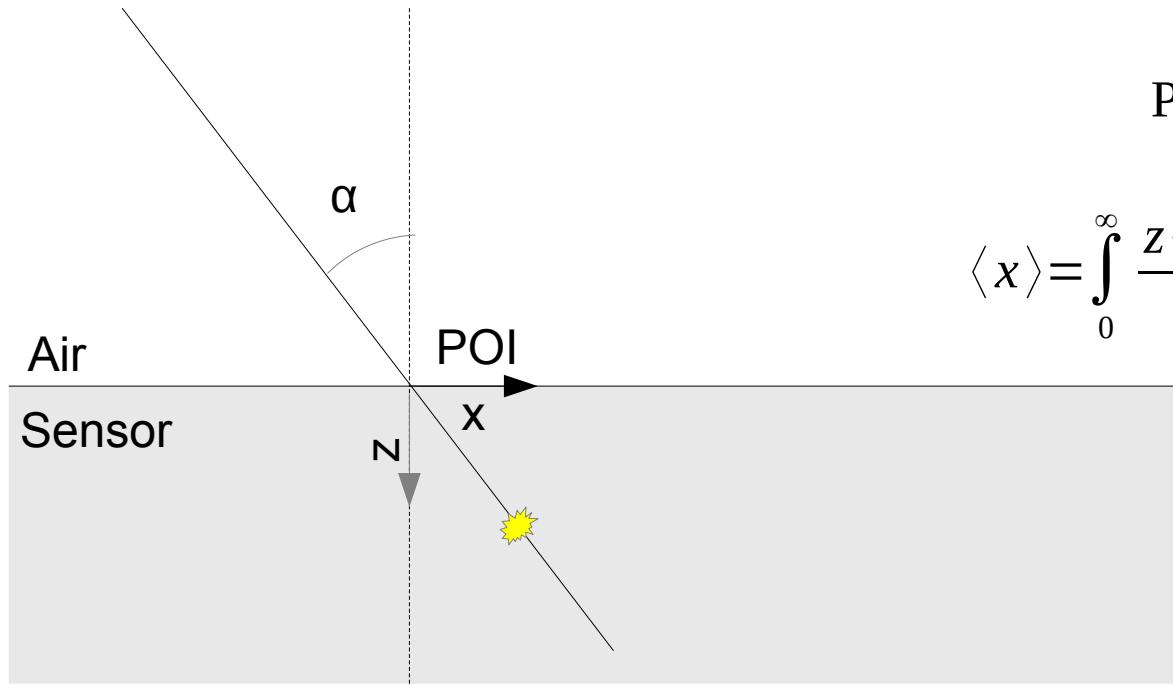
$$1 = \int_0^{\infty} P(z) dz$$

Which leads to:

$$A = \frac{\mu}{\cos(\alpha)}$$

$$P(z) = \frac{\mu}{\cos(\alpha)} \cdot e^{\frac{-\mu z}{\cos(\alpha)}}$$

$$\langle x \rangle = \int_0^{\infty} \frac{z \cdot \tan(\alpha) \cdot \mu}{\cos(\alpha)} e^{\frac{-\mu z}{\cos(\alpha)}} dz = \frac{\sin(\alpha)}{\mu}$$



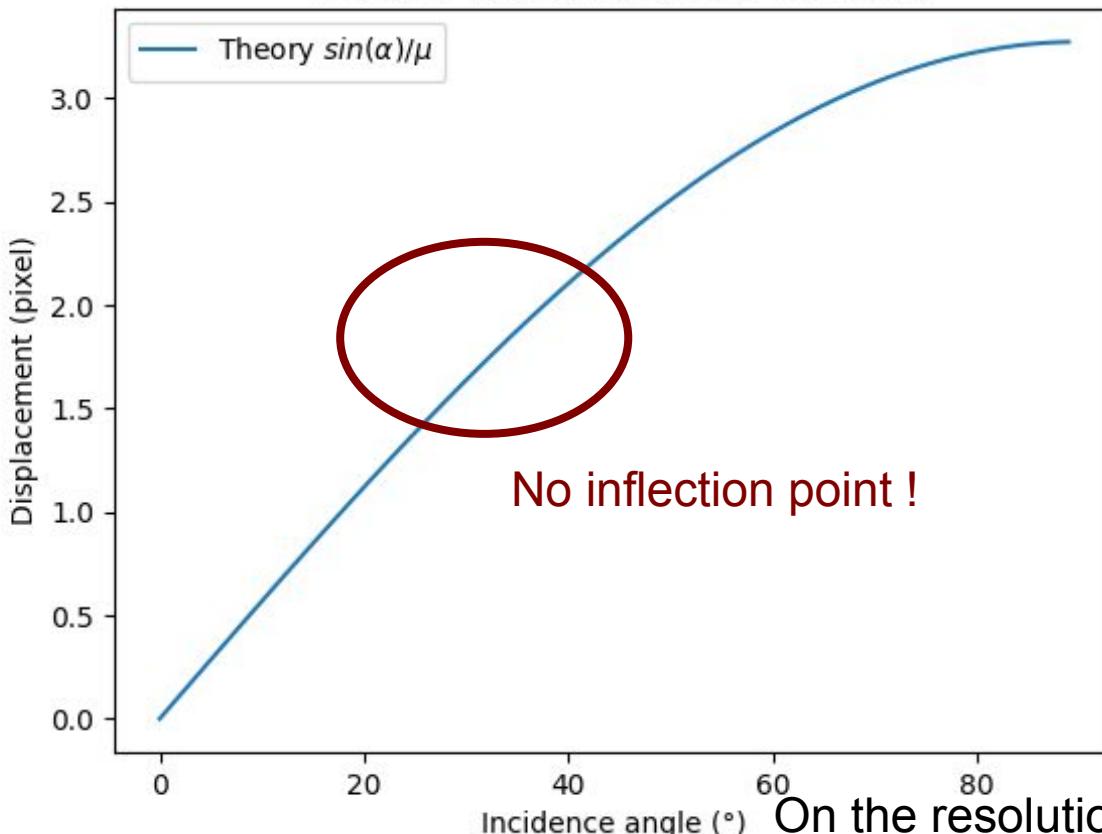
$$\Delta x = \frac{\sin(\alpha)}{\mu}$$

Thick-sensor model: quantification

- All photons are caught
- Does not depend on the sensor thickness !

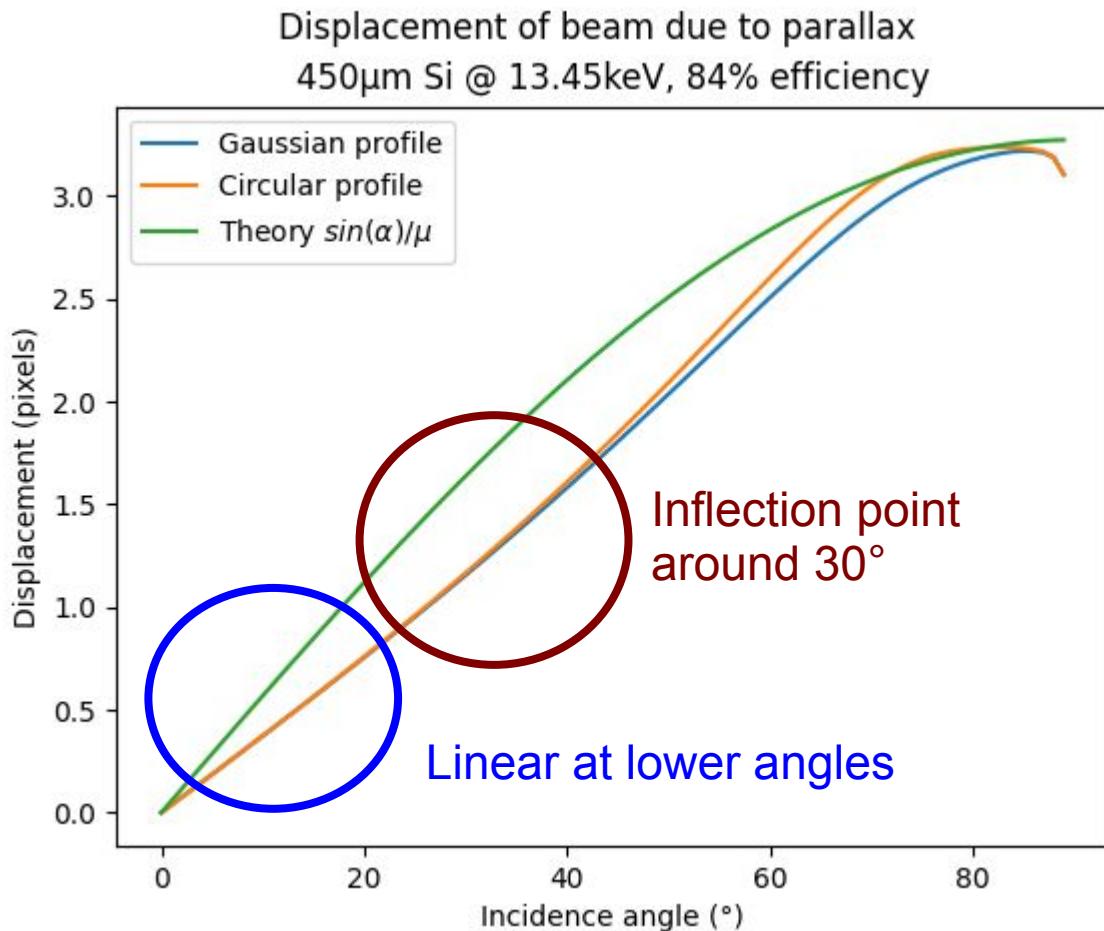
Displacement of beam due to parallax
450 μ m Si @ 13.45keV, 84% efficiency

$$\Delta x = \frac{\sin(\alpha)}{\mu}$$



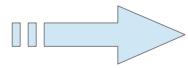
Does not match observation !
→ Displacement decreases with incident angle

On the resolution function for powder diffraction with
<https://doi.org/10.1107/S2053273321007506>



Issues:

- * Requires the beam profile
- * Numerical convolution



Search for a solution independent of the profile

Average value of an observable:

$$\langle x \rangle = \int_0^e x(z) \cdot P(z) dz$$

Geometrically, one has:

$$x(z) = z \cdot \tan(\alpha)$$

$P(z)$ follows Beer-Lambert law:

$$P(z) = A e^{\frac{-\mu z}{\cos(\alpha)}} = A e^{-\mu' z}$$

With:

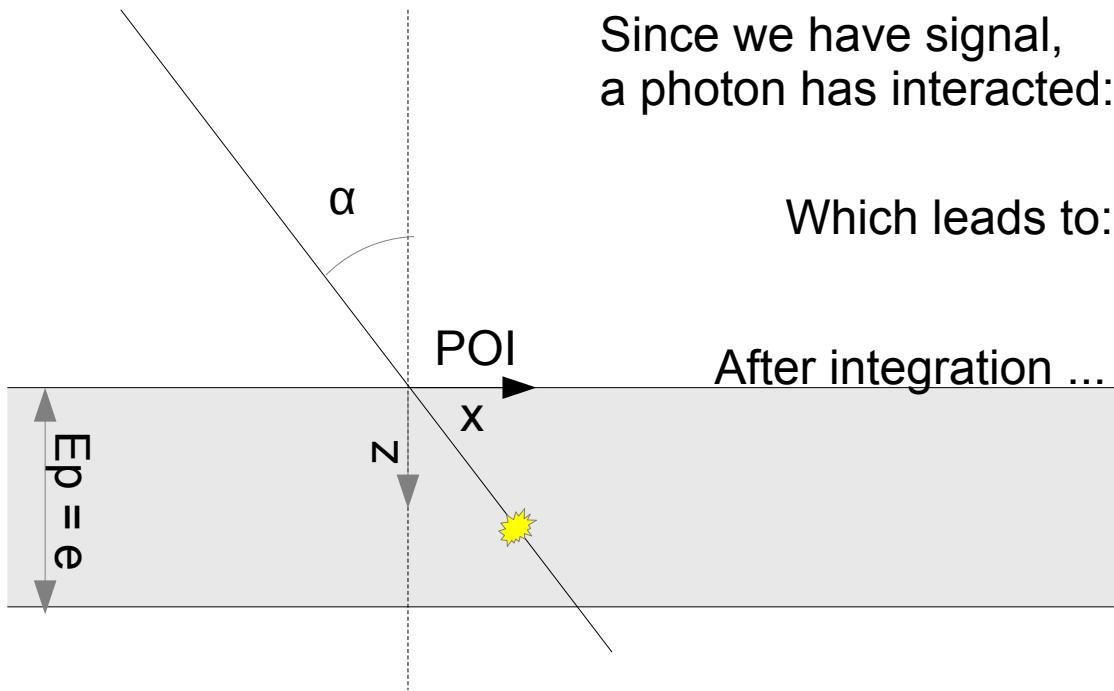
$$\mu' = \frac{\mu}{\cos(\alpha)}, A \text{ constant}$$

Since we have signal,
a photon has interacted:

$$1 = \int_0^e P(z) dz$$

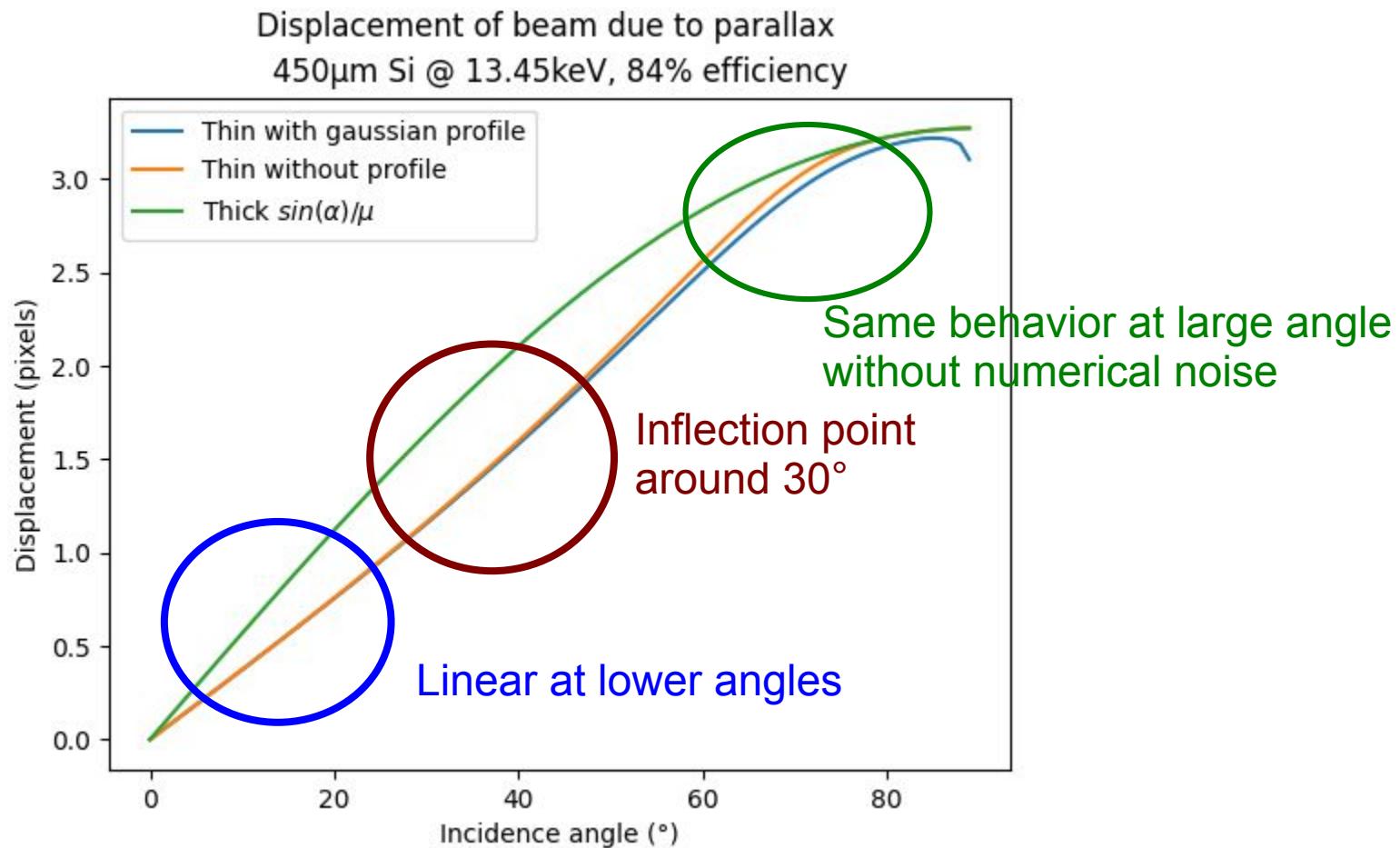
Which leads to:

$$P(z) = \mu' \cdot \frac{e^{-\mu' z}}{1 - e^{-\mu' e}}$$

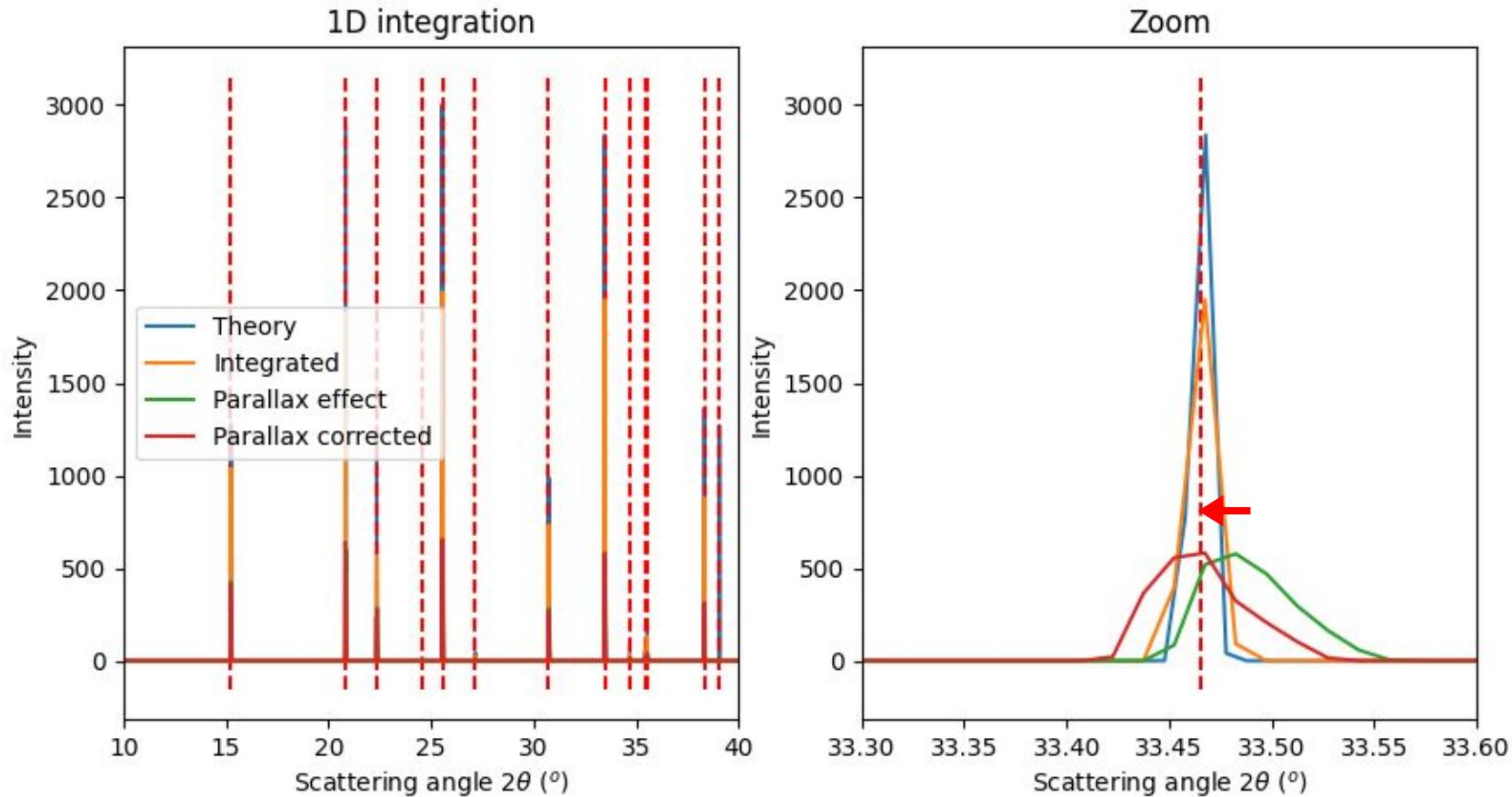


$$\langle x \rangle = \frac{\sin(\alpha) \cdot 1 - (1 + \mu' e) e^{-\mu' e}}{\mu \cdot 1 - e^{-\mu' e}}$$

Comparison of models:



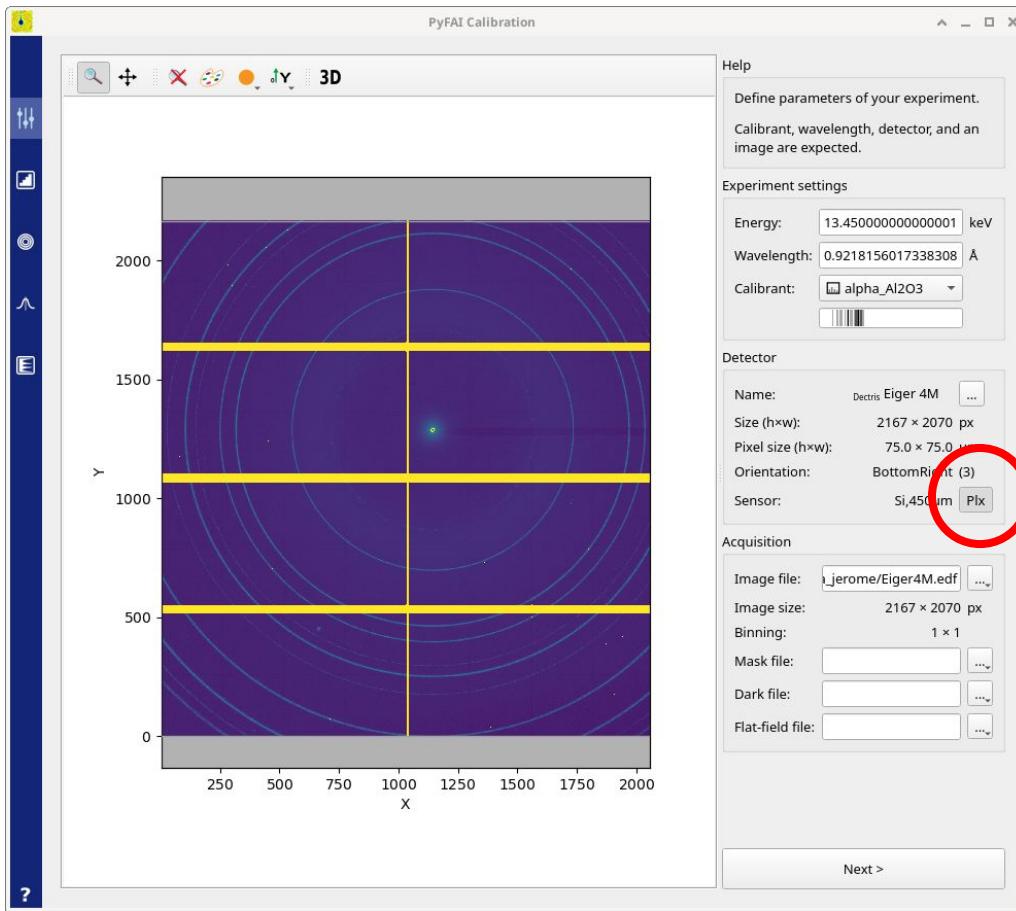
- Implementation in geometry engine of pyFAI



Makes the geometry engine of pyFAI much slower for now ...
→ rough edges still present & bugs probable !

Change of PONI-file format to cope for parallax corrections

- With pyFAI v2025.12+ there is a new PONI-file version:
 - Version 2.1 (when the parallax is disabled, backwards compatible)
 - Version 3.0 (when the parallax is enabled, backwards incompatible)



New button to activate parallax correction

Some limitations:

- Refinement does not always converge better.
- Calculation are slower for now.

- **PyFAI offers several ways to deal with parallax correction:**
 - Calculate the blurring effect via raytracing then de-smear with iterative algorithm (slow)
 - Integrate the effect in the geometry engine
- **For this the sensor composition and thickness has been tabulated.**
 - For all 300 detectors tabulated
 - Thanks to:
 - **Help of all detector manufacturers,**
 - **Detector group at ESRF**
 - **Integration work by Gudrun Lotze.**
- **All this tutorial was on the peak position ...
... not on their intensity or profile of the peaks.**
 - Absorption efficiency correction is already available in pyFAI
 - **but neither addresses the profile modification**

Questions ?

